

- 1 The points A , B and C have coordinates $(6, 1)$, $(2, 3)$ and $(-4, 3)$ respectively and O is the origin. Find, in terms of \mathbf{i} and \mathbf{j} , the vectors
- a \overrightarrow{OA} b \overrightarrow{AB} c \overrightarrow{BC} d \overrightarrow{CA}
- 2 Given that $\mathbf{p} = \mathbf{i} - 3\mathbf{j}$ and $\mathbf{q} = 4\mathbf{i} + 2\mathbf{j}$, find expressions in terms of \mathbf{i} and \mathbf{j} for
- a $4\mathbf{p}$ b $\mathbf{q} - \mathbf{p}$ c $2\mathbf{p} + 3\mathbf{q}$ d $4\mathbf{p} - 2\mathbf{q}$
- 3 Given that $\mathbf{p} = \begin{pmatrix} 3 \\ -4 \end{pmatrix}$ and $\mathbf{q} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$, find
- a $|\mathbf{p}|$ b $|2\mathbf{q}|$ c $|\mathbf{p} + 2\mathbf{q}|$ d $|3\mathbf{q} - 2\mathbf{p}|$
- 4 Given that $\mathbf{p} = 2\mathbf{i} + \mathbf{j}$ and $\mathbf{q} = \mathbf{i} - 3\mathbf{j}$, find, in degrees to 1 decimal place, the angle made with the vector \mathbf{i} by the vector
- a \mathbf{p} b \mathbf{q} c $5\mathbf{p} + \mathbf{q}$ d $\mathbf{p} - 3\mathbf{q}$
- 5 Find a unit vector in the direction
- a $\begin{pmatrix} 4 \\ 3 \end{pmatrix}$ b $\begin{pmatrix} 7 \\ -24 \end{pmatrix}$ c $\begin{pmatrix} -1 \\ 1 \end{pmatrix}$ d $\begin{pmatrix} 2 \\ 4 \end{pmatrix}$
- 6 Find a vector
- a of magnitude 26 in the direction $5\mathbf{i} + 12\mathbf{j}$,
b of magnitude 15 in the direction $-6\mathbf{i} - 8\mathbf{j}$,
c of magnitude 5 in the direction $2\mathbf{i} - 4\mathbf{j}$.
- 7 Given that $\mathbf{m} = 2\mathbf{i} + \lambda\mathbf{j}$ and $\mathbf{n} = \mu\mathbf{i} - 5\mathbf{j}$, find the values of λ and μ such that
- a $\mathbf{m} + \mathbf{n} = 3\mathbf{i} - \mathbf{j}$ b $2\mathbf{m} - \mathbf{n} = -3\mathbf{i} + 8\mathbf{j}$
- 8 Given that $\mathbf{r} = 6\mathbf{i} + c\mathbf{j}$, where c is a positive constant, find the value of c such that
- a \mathbf{r} is parallel to the vector $2\mathbf{i} + \mathbf{j}$ b \mathbf{r} is parallel to the vector $-9\mathbf{i} - 6\mathbf{j}$
c $|\mathbf{r}| = 10$ d $|\mathbf{r}| = 3\sqrt{5}$
- 9 Given that $\mathbf{p} = \mathbf{i} + 3\mathbf{j}$ and $\mathbf{q} = 4\mathbf{i} - 2\mathbf{j}$,
- a find the values of a and b such that $a\mathbf{p} + b\mathbf{q} = -5\mathbf{i} + 13\mathbf{j}$,
b find the value of c such that $c\mathbf{p} + \mathbf{q}$ is parallel to the vector \mathbf{j} ,
c find the value of d such that $\mathbf{p} + d\mathbf{q}$ is parallel to the vector $3\mathbf{i} - \mathbf{j}$.
- 10 Relative to a fixed origin O , the points A and B have position vectors $\begin{pmatrix} 3 \\ 6 \end{pmatrix}$ and $\begin{pmatrix} -5 \\ 2 \end{pmatrix}$ respectively. Find
- a the vector \overrightarrow{AB} ,
b $|\overrightarrow{AB}|$,
c the position vector of the mid-point of AB ,
d the position vector of the point C such that $OABC$ is a parallelogram.

- 11** Given the coordinates of the points A and B , find the length AB in each case.
a $A(4, 0, 9)$, $B(2, -3, 3)$ **b** $A(11, -3, 5)$, $B(7, -1, 3)$
- 12** Find the magnitude of each vector.
a $4\mathbf{i} + 2\mathbf{j} - 4\mathbf{k}$ **b** $\mathbf{i} + \mathbf{j} + \mathbf{k}$ **c** $-8\mathbf{i} - \mathbf{j} + 4\mathbf{k}$ **d** $3\mathbf{i} - 5\mathbf{j} + \mathbf{k}$
- 13** Find
a a unit vector in the direction $5\mathbf{i} - 2\mathbf{j} + 14\mathbf{k}$,
b a vector of magnitude 10 in the direction $2\mathbf{i} + 11\mathbf{j} - 10\mathbf{k}$,
c a vector of magnitude 20 in the direction $-5\mathbf{i} - 4\mathbf{j} + 2\mathbf{k}$.
- 14** Given that $\mathbf{r} = \lambda\mathbf{i} + 12\mathbf{j} - 4\mathbf{k}$, find the two possible values of λ such that $|\mathbf{r}| = 14$.
- 15** Given that $\mathbf{p} = \begin{pmatrix} 1 \\ 3 \\ -1 \end{pmatrix}$, $\mathbf{q} = \begin{pmatrix} 4 \\ -2 \\ 1 \end{pmatrix}$ and $\mathbf{r} = \begin{pmatrix} -2 \\ 5 \\ -3 \end{pmatrix}$, find as column vectors,
a $\mathbf{p} + 2\mathbf{q}$ **b** $\mathbf{p} - \mathbf{r}$ **c** $\mathbf{p} + \mathbf{q} + \mathbf{r}$ **d** $2\mathbf{p} - 3\mathbf{q} + \mathbf{r}$
- 16** Given that $\mathbf{r} = -2\mathbf{i} + \lambda\mathbf{j} + \mu\mathbf{k}$, find the values of λ and μ such that
a \mathbf{r} is parallel to $4\mathbf{i} + 2\mathbf{j} - 8\mathbf{k}$ **b** \mathbf{r} is parallel to $-5\mathbf{i} + 20\mathbf{j} - 10\mathbf{k}$
- 17** Given that $\mathbf{p} = \mathbf{i} - 2\mathbf{j} + 4\mathbf{k}$, $\mathbf{q} = -\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}$ and $\mathbf{r} = 2\mathbf{i} - 4\mathbf{j} - 7\mathbf{k}$,
a find $|2\mathbf{p} - \mathbf{q}|$,
b find the value of k such that $\mathbf{p} + k\mathbf{q}$ is parallel to \mathbf{r} .
- 18** Relative to a fixed origin O , the points A , B and C have position vectors $(-2\mathbf{i} + 7\mathbf{j} + 4\mathbf{k})$, $(-4\mathbf{i} + \mathbf{j} + 8\mathbf{k})$ and $(6\mathbf{i} - 5\mathbf{j})$ respectively.
a Find the position vector of the mid-point of AB .
b Find the position vector of the point D on AC such that $AD : DC = 3 : 1$
- 19** Given that $\mathbf{r} = \lambda\mathbf{i} - 2\lambda\mathbf{j} + \mu\mathbf{k}$, and that \mathbf{r} is parallel to the vector $(2\mathbf{i} - 4\mathbf{j} - 3\mathbf{k})$,
a show that $3\lambda + 2\mu = 0$.
 Given also that $|\mathbf{r}| = 2\sqrt{29}$ and that $\mu > 0$,
b find the values of λ and μ .
- 20** Relative to a fixed origin O , the points A , B and C have position vectors $\begin{pmatrix} 6 \\ -2 \\ -4 \end{pmatrix}$, $\begin{pmatrix} 12 \\ -7 \\ -4 \end{pmatrix}$ and $\begin{pmatrix} 6 \\ 1 \\ -8 \end{pmatrix}$ respectively.
a Find the position vector of the point M , the mid-point of BC .
b Show that O , A and M are collinear.
- 21** The position vector of a model aircraft at time t seconds is $(9 - t)\mathbf{i} + (1 + 2t)\mathbf{j} + (5 - t)\mathbf{k}$, relative to a fixed origin O . One unit on each coordinate axis represents 1 metre.
a Find an expression for d^2 in terms of t , where d metres is the distance of the aircraft from O .
b Find the value of t when the aircraft is closest to O and hence, the least distance of the aircraft from O .